# Digital Speech Processing Homework #1

Implementing Discrete Hidden Markov Model

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## Outline

- 1. HMM in Speech Recognition
- 2. Homework of HMM
  - 2.1 Training
  - 2.2 Testing
- 3. Requirements
  - 3.1 File Format
  - 3.2 Submission Requirement
- 4. Grading
- 5. Contact TAs

# HMM in Speech Recognition

In acoustic model,

- each word consists of syllables
- each syllable consists of phonemes
- each phoneme consists of some (hypothetical) states.

Each phoneme can be described by a HMM (acoustic model). Given a sequence of observation (MFCC vectors), each of them can be mapped to a corresponding state.

Hence, there are

- state transition probabilities  $(a_{ij})$  and
- observation distribution  $(b_j[o_t])$

in each phoneme acoustic model (HMM).

Usually in speech recognition we restrict the HMM to be a *left-to-right model*, and the observation distribution is assumed to be a continuous Gaussian mixture model.

### Review

- Left-to-right
- The observation distribution is a continuous Gaussian mixture model.



Figure 1: HMM from lecture 2.0

$$a_{ij} = P(q_{t+1} = j \mid q_t = i), \forall t, i, j$$
(1)  
$$b_j(A) = P(o_t = A \mid q_t = j), \forall t, A, j$$
(2)

Given  $q_t$ , the probability distributions of  $q_{t+1}$  and  $o_t$  are completely determined. (independent of other states or observation)

	Homework	Speech Recognition
$\lambda$ set	5 models	initial-final
$\lambda$	model_01-05	" < "
$\{o_t\}$	A, B, C, D, E, F	39-dim MFCC
unit	an alphabet	a time frame
observation	sequence	voice wave

# Homework of HMM



Figure 2: Training and testing models

## Problems of HMM

Training

- Basic problem 3 in lecture 4.0
  - Given observations O and an initial model λ = (A, B, π), adjust λ to maximize P(O | λ).

$$A_{ij} = a_{ij}, B_{jt} = b_j[o_t], \pi_i = P(q_1 = i)$$

• Baum-Welch algorithm

Testing

- Basic problem 2 in lecture 4.0
  - Given  $\lambda$  and O, find the best state sequences to maximize  $P(O \mid \lambda, q)$ .
- Viterbi algorithm

# Homework of HMM

Training

- Basic problem 3
- Baum-Welch algorithm: A generalized expectation-maximization (EM) algorithm<sup>1</sup>
  - Calculate  $\alpha$  (forward probabilities) and  $\beta$  (backward probabilities) given the observations
  - + Find temporary variables  $\epsilon$  and  $\gamma$  from  $\alpha$  and  $\beta$
  - Update model parameters  $\lambda' = (A', B', \pi')$

<sup>1</sup>http://en.wikipedia.org/wiki/Baum-Welch\_algorithm

### **Forward Procedure**

Forward algorithm: define a forward variable  $\alpha_t(i)$ 

$$\alpha_t(i) = P(o_1, o_2, \dots, o_t, \ q_t = i \mid \lambda)$$
(3)

= Prob[ observing  $o_1, o_2, \ldots, o_t$ , state *i* at time  $t \mid \lambda$ ] (4)

Initialization

$$\alpha_1(i) = \pi_i b_i(o_1), \ 1 \le i \le N \tag{5}$$

Induction

$$\alpha_{t+1}(j) = \left[\sum_{i=1}^{N} \alpha_t(i) a_{ij}\right] \cdot b_j(o_{t+1}),$$
  
$$1 \le t \le T - 1, \ 1 \le j \le N \quad (6)$$

Termination

$$P\left(\bar{O} \mid \lambda\right) = \sum_{i=1}^{N} \alpha_{T}(i) \tag{7}$$

Backward algorithm: define a backward variable  $\beta_t(i)$ 

$$\beta_t(i) = P(o_{t+1}, o_{t+2}, \dots, o_T \mid q_t = i, \lambda)$$
(8)

= Prob[ observing  $o_{t+1}, o_{t+2}, \dots, o_T$  | state *i* at time *t*,  $\lambda$  ] (9)

#### Initialization

$$\beta_T(i) = 1, \ 1 \le i \le N \tag{10}$$

Induction

$$\beta_t(i) = \sum_{j=1}^N a_{ij} \ b_j(o_{t+1}) \ \beta_{t+1}(j),$$
  
$$t = \{T - 1, T - 2, \dots, 1\}, \ 1 \le i \le N \quad (11)$$

Define a temporary variable  $\gamma_t(i) = P(q_t = i \mid \overline{O}, \lambda)$ 

$$\gamma_t(i) = \frac{\alpha_t(i)\beta_t(i)}{\sum_{i=1}^N \alpha_t(i)\beta_t(i)} = \frac{P\left(\bar{O}, q_t = i \mid \lambda\right)}{P\left(\bar{O} \mid \lambda\right)}$$
(12)

It should be a  $N \times T$  matrix!

The probability of transition from state *i* to state *j* given observation and model.

$$\epsilon_t(i,j) = P\left(q_t = i, q_{t+1} = j \mid \bar{O}, \lambda\right)$$
(13)

$$= \frac{\alpha_{t}(i) a_{ij} b_{j}(o_{t+1}) \beta_{t+1}(j)}{\sum_{i=1}^{N} \sum_{j=1}^{N} \alpha_{t}(i) a_{ij} b_{j}(o_{t+1}) \beta_{t+1}(j)}$$
(14)  
$$= \frac{\text{Prob} \left[\bar{O}, q_{t} = i, q_{t+1} = j \mid \lambda\right]}{P\left(\bar{O} \mid \lambda\right)}$$
(15)

In total T - 1 matrices (each  $N \times N$ )

Recall  $\gamma_t(i) = P(q_t = i \mid \overline{O}, \lambda)$ 

$$\sum_{t=1}^{T-1} \gamma_t(i) = \text{expected number of times that state } i$$
  
is visited in  $\overline{O}$  from  $t = 1$  to  $t = T - 1$  (16)  
$$\sum_{t=1}^{T-1} \epsilon_t(i,j) = \text{expected number of transitions from}$$
  
state  $i$  to state  $j$  in  $\overline{O}$  (17)

### **Re-estimate Model Parameters**

$$\lambda' = (\mathsf{A}', \mathsf{B}', \pi') \tag{18}$$

$$\pi_i = \frac{\sum \gamma_1(i)}{N}$$
, where *N* is number of samples (19)

$$a_{ij} = \frac{\sum \epsilon(i,j)}{\sum \gamma(i)} = \frac{\mathbb{E} \left[ \text{Number of transition from } i \text{ to } j \right]}{\mathbb{E} \left[ \text{Number of visiting state } i \right]}$$
(20)

$$b_i(k) = \frac{\sum_{O=k} \gamma(i)}{\sum \gamma(i)} = \frac{\mathbb{E} \left[ \text{Number of observation } O = k \text{ in state } i \right]}{\mathbb{E} \left[ \text{Number of visiting state } i \right]}$$
(21)

Accumulate  $\epsilon$  and  $\gamma$  through all samples!!! Not just the observations in one sample!

# Homework of HMM

Testing

- Basic problem 2
  - Given  $\lambda$  and O, find the best state sequences to maximize  $P(O \mid \lambda, q)$ .
- Calculate  $P(O \mid \lambda) \approx \max P(O \mid \lambda, q)$  for each of the five models
- The model with the highest probability for the most probable path usually also has the highest probability for all possible paths.

Complete procedure for Viterbi algorithm<sup>2</sup>

Initialization

$$\delta_1(i) = \pi_i b_i(o_1), \ 1 \le i \le N$$
 (22)

Recursion

$$\delta_t(j) = \max_{1 \le i \le N} [\delta_{t-1}(i) \ a_{ij}] \cdot b_j(o_t), \ 2 \le t \le T, \ 1 \le j \le N$$
(23)

Termination

$$P^* = \max_{1 \le i \le N} \left[ \delta_T(i) \right] \tag{24}$$

$$\delta_t(i) = \max_{q_1, \dots, q_{t-1}} P[q_1, q_2, \dots, q_{t-1}, q_t = i, o_1, o_2, \dots, o_t \mid \lambda]$$
(25)

= the highest probability along a certain single path ending at state *i* at time *t* for the first *t* observations, given  $\lambda$  (26)

<sup>2</sup>http://en.wikipedia.org/wiki/Viterbi\_algorithm

Homework of HMM | Testing

### Test Accuracy v.s. # of Training Iterations



Requirements

## **Provided Files**

data/train_seq_0X.txt
<ul> <li>Training data (10K observation sequences)</li> </ul>
data/test_lbl.txt
Testing labels
data/test_seq.txt
<ul> <li>Testing data (2.5K observation sequences)</li> </ul>
inc/hmm.h
Provided by TA, please work with it!
• You can load/dump models with functions within.
model_init.txt
Initial model parameters
modellist txt

• Paths to model files

#### src/test\_hmm.c

• A showcase of the usage of hmm.h

dsp-hw1
— data
test_lbl.txt
test_seq.txt
train_seq_01.txt
train_seq_02.txt
train_seq_03.txt
train_seq_04.txt
train_seq_05.txt
├── inc
└── hmm.h
└── Makefile
model_init.txt
- modellist.txt
└── src
└── test_hmm.c

#### Training

Input	1. number of iterations
	<ol><li>initial model (model_init.txt)</li></ol>
	3. observation sequences
	(train_seq_01~05.txt)

**Output** Five files of parameters for 5 models, each contains  $\lambda = (A, B, \pi)$  (e.g. model\_01~05.txt)

#### Testing

Input 1. a file of paths to the models trained in the previous step (modellist.txt)
 2. observation sequences (test\_seq.txt)
 Output best answer labels and P(O | λ) (e.g. result.txt)

./train <iter> <model\_init\_path> <seq\_path> <output\_model\_path>

iter # of iterations model\_init\_path path to the initial model params seq\_path path to sequence data output\_model\_path path to dump trained models ./test <models\_list\_path> <seq\_path> <output\_result\_path>

models\_list\_pathpath to the model list fileseq\_pathpath to sequence dataoutput\_result\_pathpath to output testing result

Compiling

make # type this in the root directory of the project

Training

./train 100 model\_init.txt data/train\_seq\_01.txt model\_01.txt

Testing

./test modellist.txt data/test\_seq.txt result.txt

#### Notice!

Command-line arguments are not fixed, read them during runtime. (e.g. Use **argv** in main function to pass the arguments.)

Also the paths in arguments need to be variable path.

# Requirements

File Format

The given data/train\_seq\_01~05.txt and data/test\_seq.txt look like this.

ACCDDDDFFCCCCBCFFFCCCCCEDADCCAEFCCCACDDFFCCDDFFCCD
 CABACCAFCCFFCCCDFFCCCCDFFCDDDDFCDDCCFCCCEFFCCCCBF
 ABACCCDDCCCDDDFBCCCCCDDAACFBCCBCCCCCCFFFCCCCDBF
 AAABBBCCFFBDCDDFFACDCDFCDDFFFFCDFFFCCDCFFFFCCCD
 AACCDCCCCCCCDCBCBFFFCDCDCDAFBCDCFFCCDCCEACDBAFFF
 AAABBACCFFBDCDCBFFFCDCDCDAFBCDCFFCCDCCEACDBAFFF

Each of the former has 10000 sequences and the latter has 2500 sequences.

## Model Format 1/2

initial: 6

$$\pi = [\pi_1, \pi_2, \pi_3, \pi_4, \pi_5, \pi_6]$$

transition: 6

$$A = \begin{bmatrix} a_{11} & \dots & a_{16} \\ \vdots & \ddots & \vdots \\ a_{61} & \dots & a_{66} \end{bmatrix}$$

observation: 6<sup>3</sup>

$$B = \begin{bmatrix} b_1(o_1) & \dots & b_6(o_1) \\ \vdots & \ddots & \vdots \\ b_1(o_6) & \dots & b_6(o_6) \end{bmatrix}$$

<sup>3</sup>The sum of column is 1 here.

Requirements | File Format

A model file (e.g. model\_0X.txt) should look like this.

initia	al: 6					
0.2	0.1	0.2	0.2	0.2	0.1	
trans	ition: 6					
0.3	0.3	0.1	0.1	0.1	0.1	
0.1	0.3	0.3	0.1	0.1	0.1	
0.1	0.1	0.3	0.3	0.1	0.1	
0.1	0.1	0.1	0.3	0.3	0.1	
0.1	0.1	0.1	0.1	0.3	0.3	
0.3	0.1	0.1	0.1	0.1	0.3	
observ	vation: 6	5				
0.2	0.2	0.1	0.1	0.1	0.1	
0.2	0.2	0.2	0.2	0.1	0.1	
0.2	0.2	0.2	0.2	0.2	0.2	
0.2	0.2	0.2	0.2	0.2	0.2	
0.1	0.1	0.2	0.2	0.2	0.2	
0.1	0.1	0.1	0.1	0.2	0.2	

The given modellist.txt looks like this.

```
1 model_01.txt
2 model_02.txt
3 model_03.txt
4 model_04.txt
5 model_05.txt
```

Your testing program should be able to read a list like this and load models from the specified paths for testing. (Don't worry! If you use hmm.h, all of these are done by calling function load\_models(). For more details please refer to hmm.h.)

Your testing program should output these to the specific path (e.g. **result.txt**) given as a command-line argument while executing the program.

```
1 model_01.txt 7.822367e-34
2 model_05.txt 1.094896e-40
3 model_01.txt 7.928724e-33
4 model_02.txt 4.262100e-37
5 model_02.txt 5.914689e-42
6 ...
```

Each line consists of the hypothesis model and its likelihood. They should be separated by a space.

#### The first few lines of the given data/test\_lbl.txt looks like this.

model\_01.txt
model\_05.txt
model\_01.txt
model\_01.txt
model\_02.txt
model\_02.txt
model\_02.txt
...

The Makefile you submit should be capable to compile your program using make. The provided one can compile train.c and test.c in directory src into two executables train and test.

```
.PHONY: all clean run
    CC=gcc
2
    CELAGS=-std=c99 -02
3
    LDFLAGS=-lm
4
    TARGET=train test
5
6
    all: $(TARGET)
7
8
    train: src/train.c
9
        $(CC) -o $@ $^ $(CFLAGS) $(LDFLAGS) -Iinc
10
    test: src/test.c
12
        $(CC) -o $@ $^ $(CFLAGS) $(LDFLAGS) -Iinc
13
14
    clean:
15
        rm -f $(TARGET)
16
```

Please write a **one-page** report in **PDF** format, name it **report.pdf** and submit with your source code.

State your name, student ID and any challenges you encounter or attempts you try. A good report may grant you bonus of extra 5%.

#### All of your source code files must be placed under inc/ and src/.

Let's say you only have two implementation files and use the functions provided in hmm.h. You should put your source code under src/ and leave hmm.h in inc/.

Requirements

Submission Requirement

- 1. Create a directory named hw1\_[STUDENT\_ID].
- 2. Put
  - · inc∕
  - Makefile
  - model\_init.txt
  - report.pdf
  - · src/

into the directory.  $^{\rm 4}$ 

- Compress the directory into a ZIP file named hw1\_[STUDENT\_ID].zip.
- 4. Upload this ZIP file to CEIBA.

<sup>&</sup>lt;sup>4</sup>Put every source code files in **inc/** and **src/**.

Let's say your student ID is r01234567.

```
hw1 r01234567.zip
hw1_r01234567
        inc
        └── [*.h or *.hpp]
        Makefile
        model init.txt
        report.pdf
        src
        └── [*.c, *.cc or *.cpp]
```

# Grading

Your training and testing program will be tested respectively. We will specify **100** as the number of iterations while testing your training program. And each of your program is allowed to run for 1 min.

Here's TA's environment.

Kernel Linux 5.3.1-arch1-1-ARCH <sup>5</sup> Processors Intel Core i7-9700K (2 Cores) RAM 4096 MB GCC Version 9.1.0

<sup>&</sup>lt;sup>5</sup>You can download the OVA file here if need be: https://ppt.cc/fl7drx. The user is *root* and its password is *ntudsp* 

File Format 20%

- ZIP file name
- directory name
- separated header and implementation files
- Makefile
- model\_init.txt

Program 20%

- compiled and executed without error
- output files generated after execution

Report 10%

and bonus of extra 5% for the impressive ones

Accuracy 50%

30% for your training program and 20% for your testing program

#### Due on November 1, 2019

You are still allowed to submit after 2019-11-01 23:59. The penalty for late submission is an exponential decay with decay rate 1.5%<sup>6</sup> of the maximum grade applicable for the assignment, for each hour that the assignment is late.

An assignment submitted more than 3 days after the deadline will have a grade of zero recorded for that assignment.

$$SCORE_{final}(hr) = \begin{cases} SCORE_{original} \times 0.985^{hr} &, hr \le 72\\ 0 &, hr > 72 \end{cases}$$

<sup>6</sup>less than 70% after 24 hrs, 48% for 48 hrs and 33% for 72 hrs

#### File Frmat

- All of your source code files should be placed under inc/ and src/.
- model\_init.txt must be submitted, even if it's not needed for your program.

#### Program

- Make sure your program can be compiled with the Makefile you submit.
- The paths in command-line arguments have to be relative path.
- Each of your program is allowed to run for 1 min.

#### Accuracy

• Make sure your training program saves models within time limit.

#### Should you have any questions, please read the FAQ<sup>7</sup> first.

<sup>&</sup>lt;sup>7</sup>http://speech.ee.ntu.edu.tw/DSP2019Autumn/hw1/FAQ.html

Any form of cheating, lying, or plagiarism will not be tolerated.

# Questions?

Should you have any question or need help,

- send email to ntudsp\_2019fall\_ta@googlegroups.com
- and use "[HW1]" as the subject line prefix

Or come to EE2 R531, and don't forget to inform us by email, thanks!

林美即	Tue.	14:00 - 17:00
你我主	Thr.	9:00 - 12:00
林政高	Mon.	10:00 - 12:00
小以家	Thr.	15:00 - 18:00

Office hours