More about Validation Set

I used a validation set, but my model still overfitted?

Validation Set

Training Set \mathcal{D}_{train}

Model
$$\mathcal{H}_1$$
 $h_1^* = arg \min_{h \in \mathcal{H}_1} L(h, \mathcal{D}_{train})$

Model
$$\mathcal{H}_2$$
 $h_2^* = arg \min_{h \in \mathcal{H}_2} L(h, \mathcal{D}_{train})$

Model
$$\mathcal{H}_3$$
 $h_3^* = arg \min_{h \in \mathcal{H}_3} L(h, \mathcal{D}_{train})$

Validation Set \mathcal{D}_{val}

$$L(h_1^*, \mathcal{D}_{val}) = 0.9$$

$$L(h_2^*, \mathcal{D}_{val}) = 0.7$$

$$L(h_3^*, \mathcal{D}_{val}) = 0.5$$

Testing Set \mathcal{D}_{test}

Approximation of \mathcal{D}_{all}

Training Set \mathcal{D}_{train}

Model
$$\mathcal{H}_1$$
 $h_1^* = arg \min_{h \in \mathcal{H}_1} L(h, \mathcal{D}_{train})$

Model
$$\mathcal{H}_2$$
 $h_2^* = arg \min_{h \in \mathcal{H}_2} L(h, \mathcal{D}_{train})$

Model
$$\mathcal{H}_3$$
 $h_3^* = arg \min_{h \in \mathcal{H}_3} L(h, \mathcal{D}_{train})$

Validation Set $\overline{\mathcal{D}_{val}}$

$$L(h_1^*, \mathcal{D}_{val}) = 0.9$$

$$L(h_2^*, \mathcal{D}_{val}) = 0.7$$

$$L(h_3^*, \mathcal{D}_{val}) = 0.5$$

$$\mathcal{H}_{val} = \{h_1^*, h_2^*, h_3^*\} \qquad h^* = \arg\min_{h \in \mathcal{H}_{val}} L(h, \mathcal{D}_{val})$$

Using validation set to select model =

considered as "training" by \mathcal{D}_{val}

Your model is $\mathcal{H}_{val} = \{h_1^*, h_2^*, h_3^*\}$

Using validation set to select model = considered as "training" by \mathcal{D}_{val} Your model is $\mathcal{H}_{val} = \{h_1^*, h_2^*, h_3^*\}$

$$\begin{split} L\big(h^{train}, \mathcal{D}_{all}\big) - L\big(h^{all}, \mathcal{D}_{all}\big) &\leq \delta \\ P\big(\mathcal{D}_{train} \ is \ \pmb{bad}\big) &\leq |\mathcal{H}| \cdot 2exp(-2N\varepsilon^2) \\ L\big(h^{val}, \mathcal{D}_{all}\big) - L\big(h^{all}, \mathcal{D}_{all}\big) &\leq \delta \\ P\big(\mathcal{D}_{val} \ is \ \pmb{bad}\big) &\leq |\mathcal{H}_{val}| \cdot 2exp(-2N_{val}\varepsilon^2) \\ &\uparrow \\ \text{It is small.} \end{split}$$

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