

Linear System =
System of Linear Equations

System of Linear Equations

多元一次聯立方程式

m equations

$$\begin{cases} a_{11}x_1 + a_{12}x_2 + \cdots + a_{1n}x_n = b_1 \\ a_{21}x_1 + a_{22}x_2 + \cdots + a_{2n}x_n = b_2 \\ \vdots \\ a_{m1}x_1 + a_{m2}x_2 + \cdots + a_{mn}x_n = b_m \end{cases}$$

coefficient

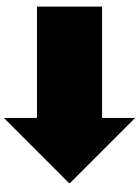
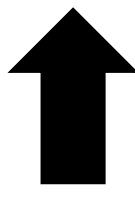
n variables

In this course, m and n can be large

Linear System

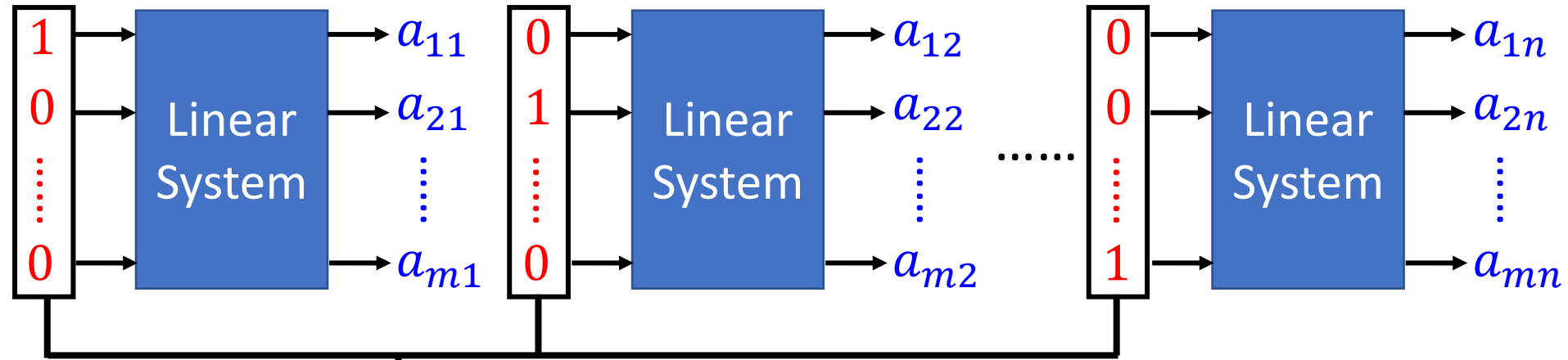
= System of Linear Equations



Next page   Trivial!

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A linear system \rightarrow A system of linear equations

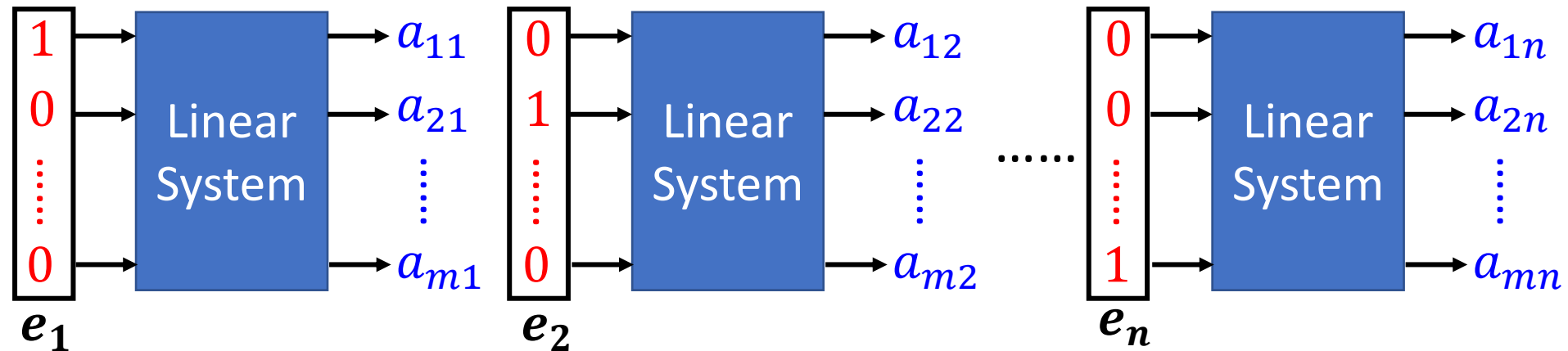


standard (unit) vector

(only one element is "1",
the rest elements are "0")



A linear system \rightarrow A system of linear equations



standard (unit) vector

(only one element is "1",
the rest elements are "0")

$$\begin{aligned} \mathbf{v} = \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} &= v_1 \begin{bmatrix} 1 \\ 0 \end{bmatrix} + v_2 \begin{bmatrix} 0 \\ 1 \end{bmatrix} \\ &= v_1 \mathbf{e}_1 + v_2 \mathbf{e}_2 \end{aligned}$$



A linear system \rightarrow A system of linear equations

